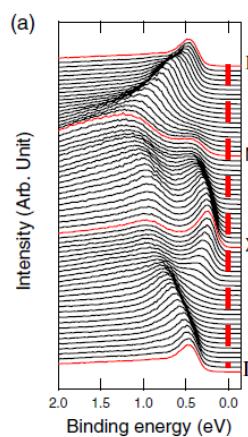
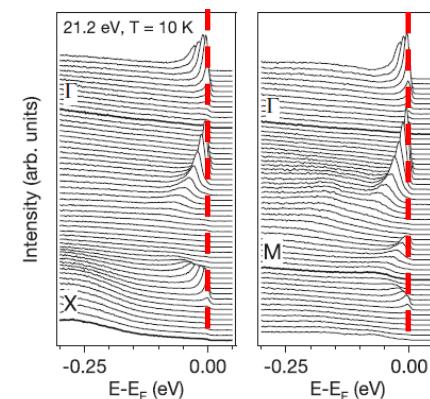
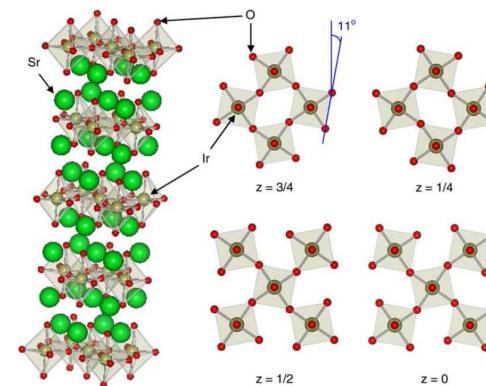


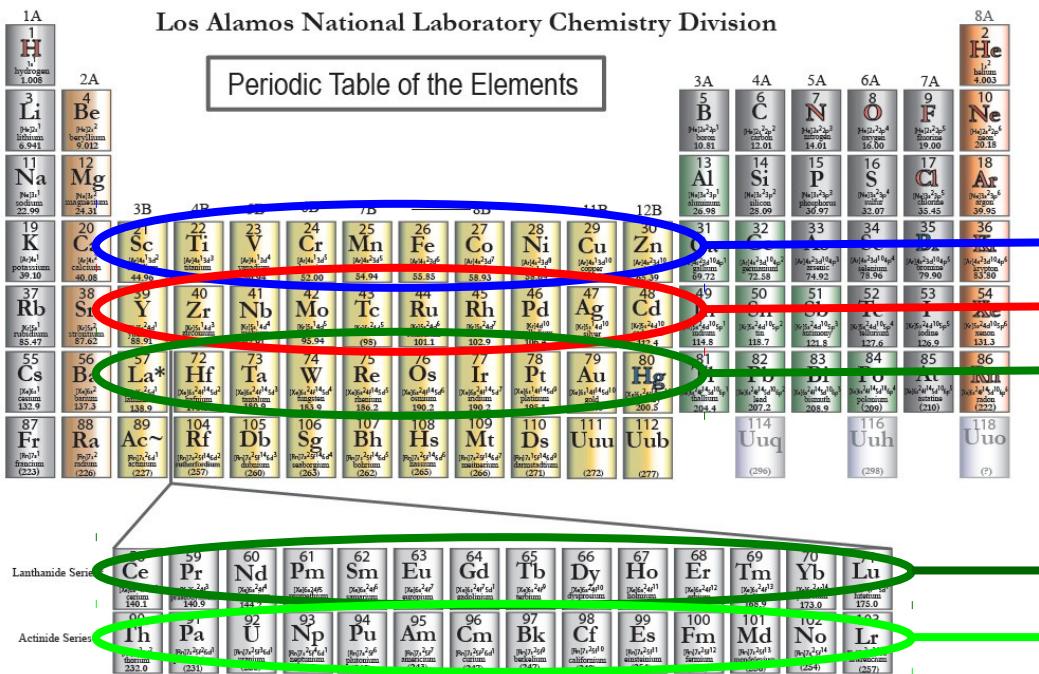
# Why is $\text{Sr}_2\text{IrO}_4$ insulating and $\text{Sr}_2\text{RhO}_4$ is not? Effects of spin-orbit coupling and structural distortions



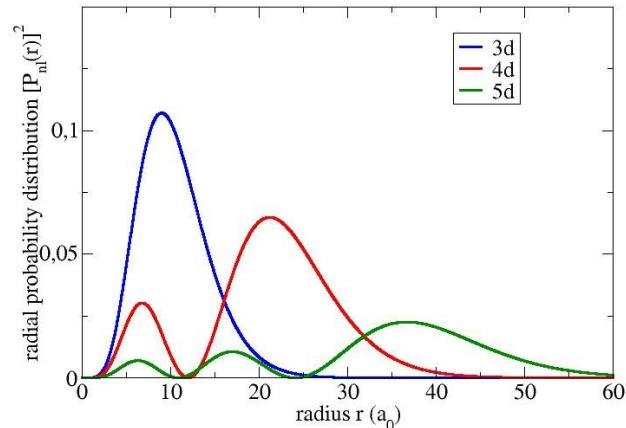
$\text{Sr}_2\text{IrO}_4$



$\text{Sr}_2\text{RhO}_4$



3d  
4d  
5d



4f Lanthanides

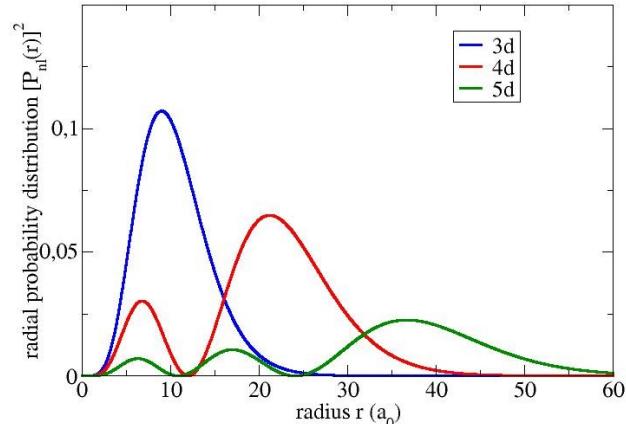
5f Actinides

Correlated materials are

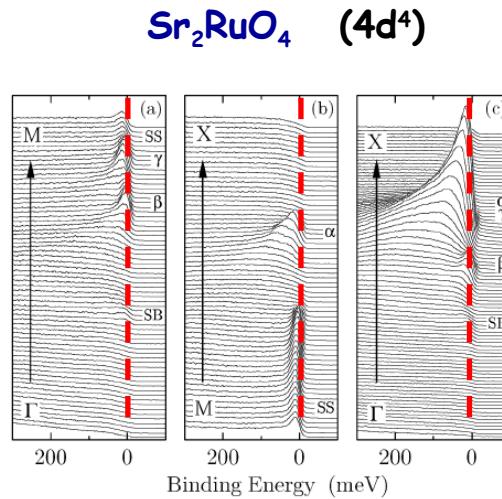
- 3d transition metals and & their oxides
- Rare earth (Lanthanides 4f) and Actinides (5f)
- 4d transition metal oxides :  $\text{Sr}_2\text{RuO}_4$ ,  $\text{SrTcO}_3$ ...

<b>3d</b>	<b>21 Sc</b> $[Ar]4s^2 3d^2$ scandium 44.96	<b>22 Ti</b> $[Ar]4s^2 3d^3$ titanium 47.88	<b>23 V</b> $[Ar]4s^2 3d^4$ vanadium 50.94	<b>24 Cr</b> $[Ar]4s^1 3d^5$ chromium 52.00	<b>25 Mn</b> $[Ar]4s^2 3d^5$ manganese 54.94	<b>26 Fe</b> $[Ar]4s^2 3d^6$ iron 55.85	<b>27 Co</b> $[Ar]4s^2 3d^7$ cobalt 58.93	<b>28 Ni</b> $[Ar]4s^2 3d^8$ nickel 58.69	<b>29 Cu</b> $[Ar]4s^1 3d^9$ copper 63.55	<b>30 Zn</b> $[Ar]4s^2 3d^{10}$ zinc 65.39
<b>4d</b>	<b>39 Y</b> $[Ar]4s^2 4d^1$ yttrium 88.91	<b>40 Zr</b> $[Ar]4s^2 4d^2$ zirconium 91.22	<b>41 Nb</b> $[Ar]4s^2 4d^4$ niobium 92.91	<b>42 Mo</b> $[Ar]4s^2 4d^5$ molybdenum 95.94	<b>43 Tc</b> $[Ar]4s^2 4d^5$ technetium (98)	<b>44 Ru</b> $[Ar]4s^2 4d^6$ ruthenium 101.1	<b>45 Rh</b> $[Ar]4s^2 4d^7$ rhodium 102.9	<b>46 Pd</b> $[Ar]4s^2 4d^10$ palladium 106.4	<b>47 Ag</b> $[Ar]4s^2 4d^{10}$ silver 107.9	<b>48 Cd</b> $[Ar]4s^2 4d^{10}$ cadmium 112.4
<b>5d</b>	<b>57 La*</b> $[Ar]4s^2 5d^1$ lanthanum 138.9	<b>72 Hf</b> $[Ar]4s^2 4f^1 5d^2$ hafnium 178.5	<b>73 Ta</b> $[Ar]4s^2 4f^1 4d^3$ tantalum 180.9	<b>74 W</b> $[Ar]4s^2 4f^1 4d^4$ tungsten 183.9	<b>75 Re</b> $[Ar]4s^2 4f^1 4d^5$ rhenium 186.2	<b>76 Os</b> $[Ar]4s^2 4f^1 4d^6$ osmium 190.2	<b>77 Ir</b> $[Ar]4s^2 4f^1 4d^5 5d^1$ iridium 190.2	<b>78 Pt</b> $[Ar]4s^2 4f^1 4d^6 5d^0$ platinum 195.1	<b>79 Au</b> $[Ar]4s^2 4f^1 4d^6 5d^1$ gold 197.0	<b>80 Hg</b> $[Ar]4s^2 4f^1 5d^1 6s^0$ mercury 200.5

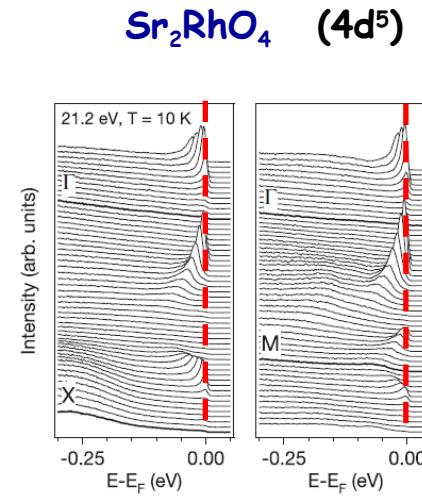
4d states are considered as less localized and correlated than 3d  
 5d states are considered as less localized and correlated than 4d



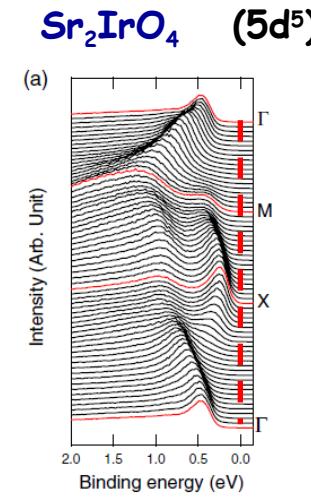
### Angle Resolved Photo-Emission Spectroscopy (ARPES) spectra for :



Damascelli et al,  
Phys Rev Lett 85, 5194 (2000)



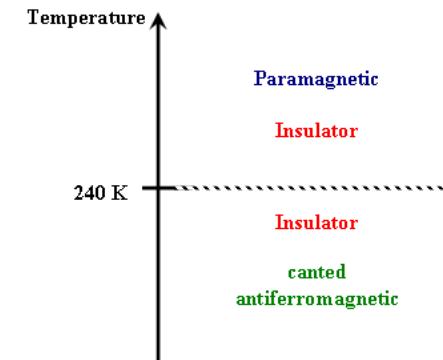
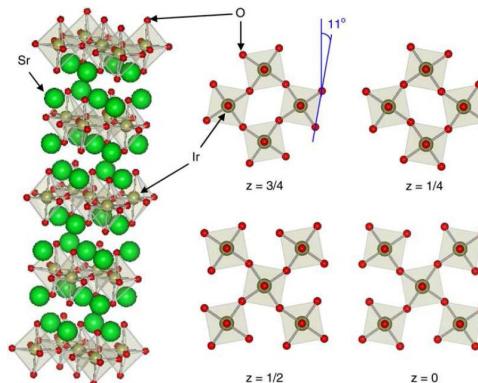
Baumberger et al,  
Phys Rev Lett 96, 246402 (2006)



Kim et al,  
Phys Rev Lett 101, 076402 (2009)

- A structure similar to  $\text{La}_2\text{CuO}_4$  or  $\text{Sr}_2\text{RuO}_4$  but with distortions :

$\text{IrO}_6$  octahedra are rotated around the z axis by about  $11^\circ$ .



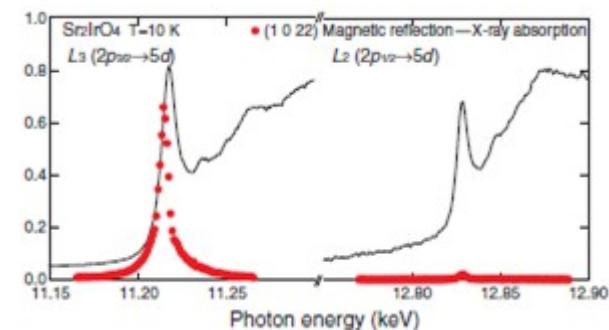
Klein & Terasaki, J. Phys.: Cond. Mat. 20 (2008)

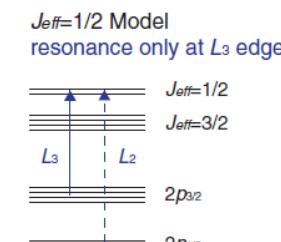
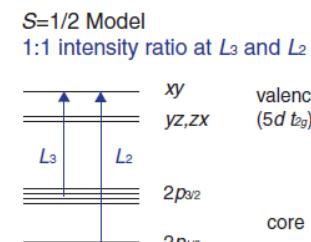
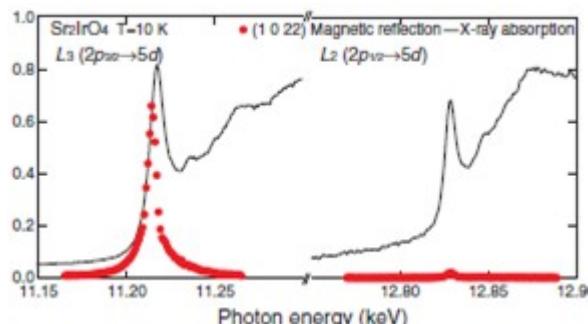
- An insulator at all temperatures but Ir atoms accommodate 5 electrons.

An optical gap at 300 K (room temperature) of 0.26 eV. Moon et al, Phys Rev B 80, 195110 (2009)

- An important role of the spin-orbit coupling ( $\zeta_{SO} \sim 0.4$  eV) according to resonant X-ray scattering.

Kim et al, Science 323, 1329 (2009)





Kim et al, Phys Rev Lett 101, 076402 (2009)  
Kim et al, Science 323, 1329 (2009)

The spin-orbit interaction is a relativistic correction to the Schrödinger equation.

$$H_{SO} = \frac{\hbar^2}{2m_0^2c^2} \mathbf{S} \cdot [\nabla V(\mathbf{r}) \times \mathbf{p}] \quad \text{and for an atom: } H_{SO} = \frac{1}{2m_0^2c^2} \frac{1}{r} \frac{dV}{dr} (\mathbf{L} \cdot \mathbf{S}) = \zeta_{SO} \mathbf{L} \cdot \mathbf{S}.$$

The energy splitting induced by the spin-orbit coupling scales roughly as Z<sup>4</sup>.

Iron (Fe)                          (Z= 26)       $\zeta_{SO} \sim 0.050$  eV

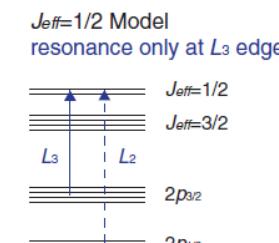
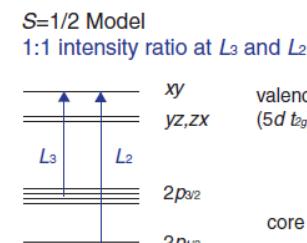
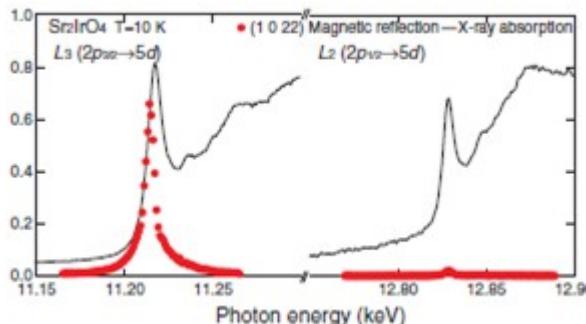
Copper (Cu)                          (Z= 29)       $\zeta_{SO} \sim 0.103$  eV

Ruthenium (Ru)                          (Z= 44)       $\zeta_{SO} \sim 0.161$  eV

Rhodium (Rh)                          (Z= 45)       $\zeta_{SO} \sim 0.191$  eV

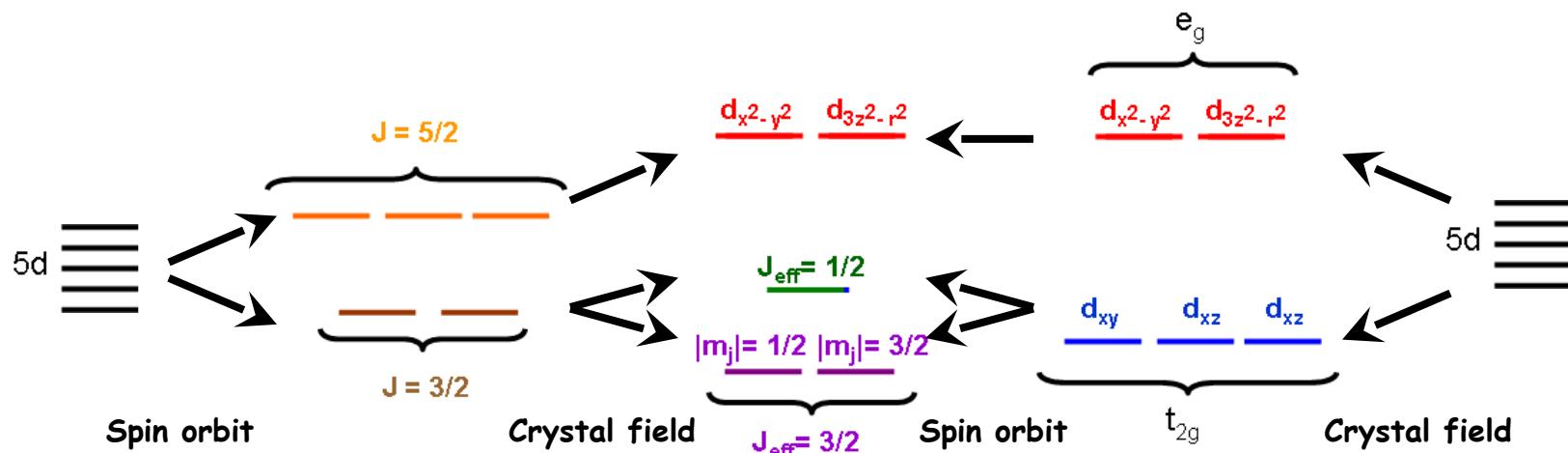
Iridium (Ir)                          (Z= 77)       $\zeta_{SO} \sim 0.4$  eV

Bismuth (Bi)                          (Z= 83)       $\zeta_{SO} \sim 1.5$  eV

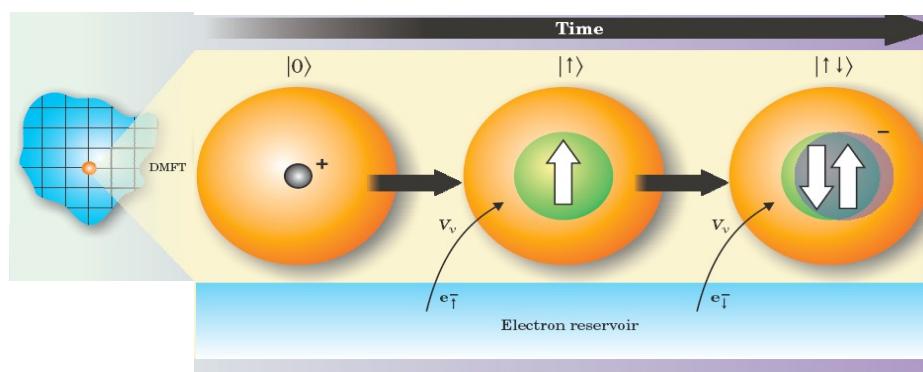
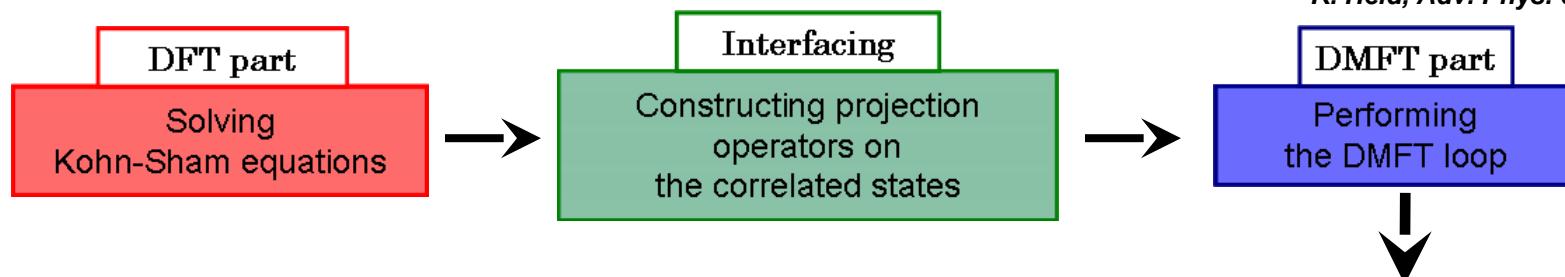


Kim et al, Phys Rev Lett 101, 076402 (2009)  
Kim et al, Science 323, 1329 (2009)

Because of the crystal field induced by the oxygen, the 5d states are split into e<sub>g</sub>, J<sub>eff</sub>=1/2 and J<sub>eff</sub>=3/2 multiplets.



Lichtenstein & Katsnelson, PRB 57, 6884 (1998) ; Anisimov et al, J. Phys. Cond Mat. 9, 7359 (1997)  
K. Held, Adv. Phys. 56, 829 (2007)

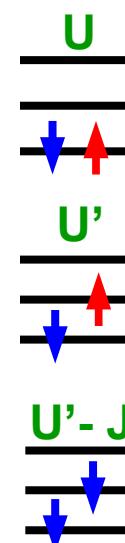


The lattice problem is mapped onto a local impurity problem (AIM).

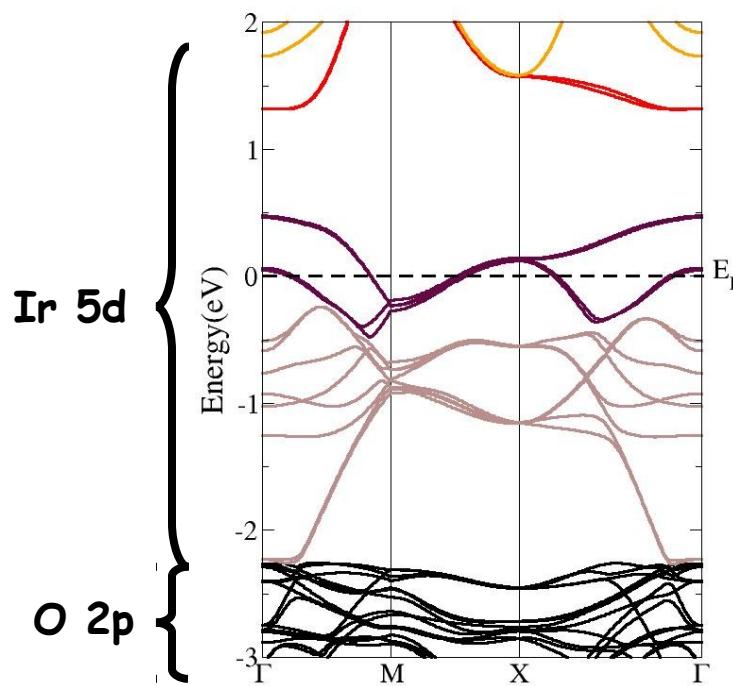
Solution of the AIM by Continuous Time QMC.  
Parameters from constrained RPA calculations.

Georges et al, Rev Mod Phys 68, 13 (1996)

$$\begin{aligned}
H = & U \sum_m n_{m\uparrow} n_{m\downarrow} \\
& + U' \sum_{m>n,\sigma} n_{m\sigma} n_{n-\sigma} \\
& + (U' - J) \sum_{m>n,\sigma} n_{m\sigma} n_{n\sigma}
\end{aligned}$$

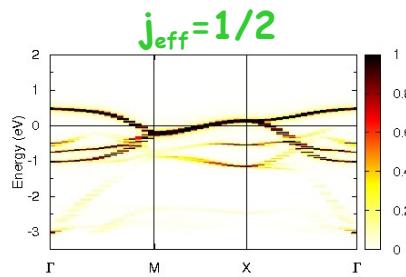


Self consistent implementation in Wien2K: M. Aichhorn et al., PRB 2009, PRB 2011

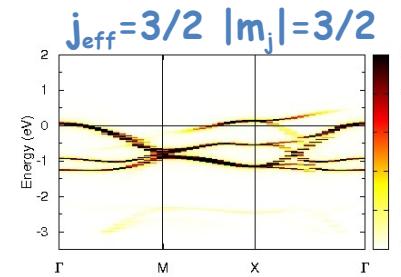


4 bands cross the Fermi level:  
a **metallic** Kohn-Sham band structure

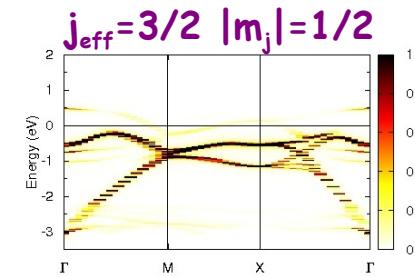
$$\begin{aligned} j_{\text{eff}} &= 1/2 \\ j_{\text{eff}} &= 3/2 \end{aligned}$$



$$n = 1.14$$



$$n = 1.96$$



$$n = 2.00$$

Distortions and SO coupling produces an effective one-band problem

Interaction parameters estimated by cRPA:

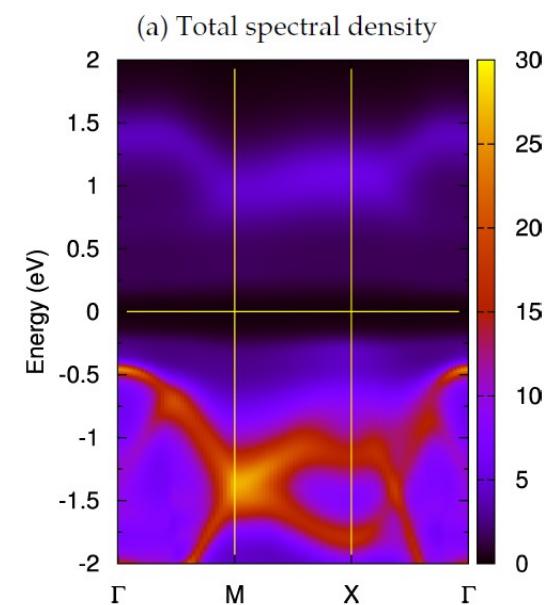
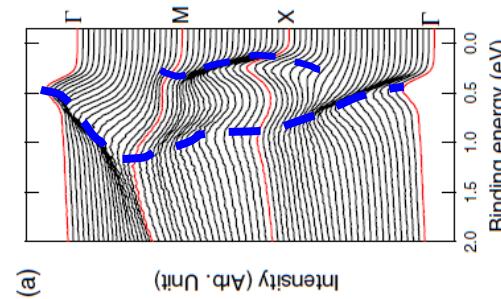
$$U = 2.2 \text{ eV} \quad J = 0.3 \text{ eV}$$



Insulating state with a gap of about 0.26 eV

Comparison with experimental spectral function obtained with ARPES (at 100K) :

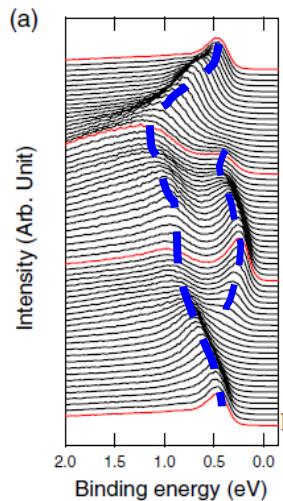
Kim et al, Phys Rev Lett 101, 076402 (2009)



C. Martins, M. Aichhorn, L. Vaugier, and S. Biermann, PRL 107, 266404 (2011)

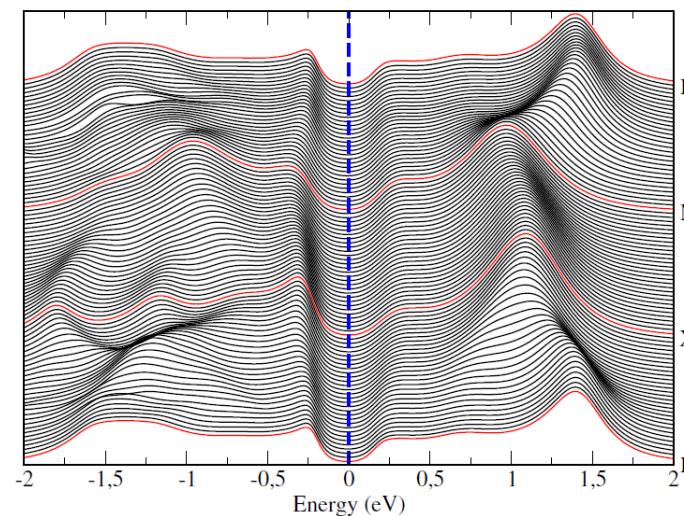
## Experimental spectrum

Kim et al, Phys Rev Lett 101, 076402 (2009)

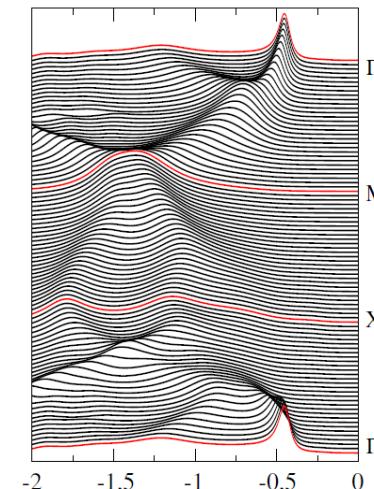


## Calculated orbitally resolved spectral density

Orbital  $j_{\text{eff}}=1/2$



Orbital  $j_{\text{eff}}=3/2$



$\text{Sr}_2\text{IrO}_4$  is a  $j_{\text{eff}}=1/2$  Mott insulator. ( $U=2.2$  eV and  $J=0.3$  eV)

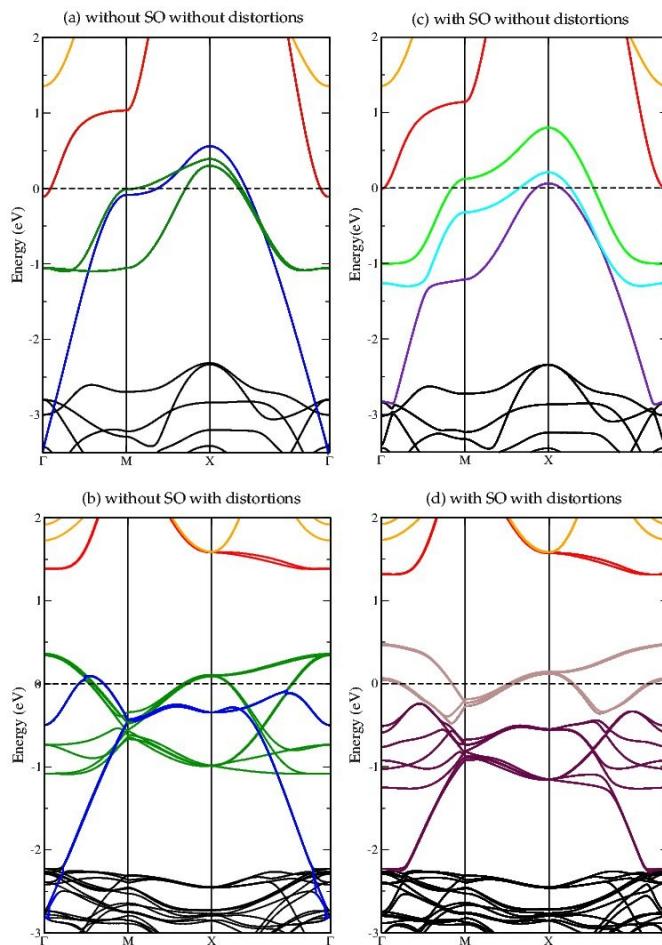
neither a magnetic order, nor an orbital order but a "spin-orbital order"

The suppression of spin-orbital fluctuations is a consequence of the combined effect of :

- Spin orbit coupling ( $\zeta_{\text{SO}} \sim 0.4$  eV)

- the structural distortions (rotation of  $11^\circ$  of the  $\text{IrO}_6$  octahedra)

10



Without structural distortions:

A  $j_{\text{eff}}=1/2$  Mott insulator is obtained for:

$$U > 3.0 \text{ eV}$$

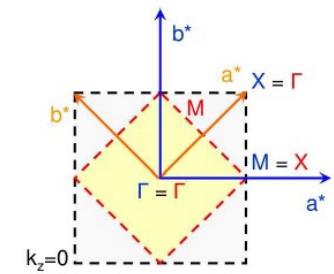
---  $dx^2-y^2$

---  $d3z^2-r^2$

---  $J_{\text{eff}}=1/2$

---  $J_{\text{eff}}=3/2 \quad |m_j|=3/2$

---  $J_{\text{eff}}=3/2 \quad |m_j|=1/2$

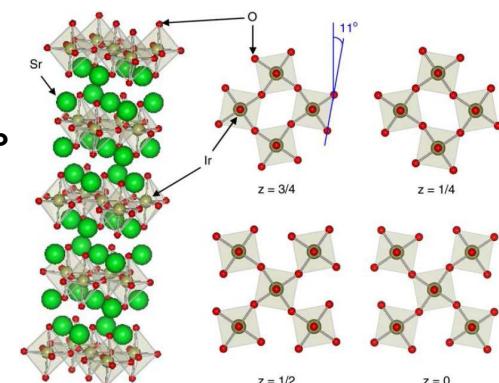


- The same crystal structure as  $\text{Sr}_2\text{IrO}_4$ :

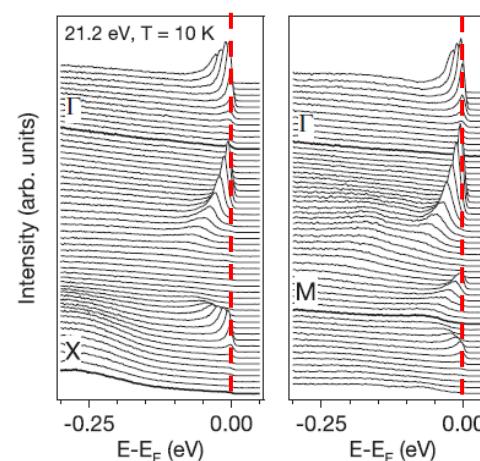
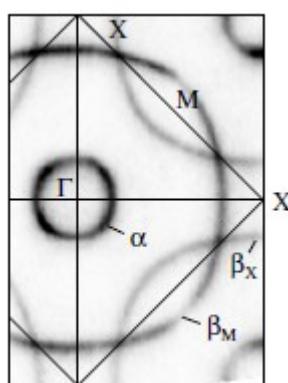
$\text{RhO}_6$  octahedra are rotated around the z axis by about  $11^\circ$

$$a(\text{Sr}_2\text{RhO}_4) = 5.44 \text{ \AA} ; c(\text{Sr}_2\text{RhO}_4) = 25.75 \text{ \AA}$$

$$a(\text{Sr}_2\text{IrO}_4) = 5.49 \text{ \AA} ; c(\text{Sr}_2\text{IrO}_4) = 25.77 \text{ \AA}$$



- A paramagnetic metal down to 36 mK. Moon et al. Phys Rev B 74, 113104 (2006)

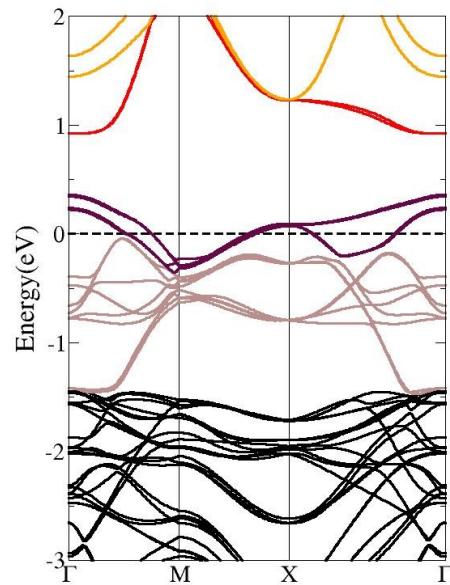
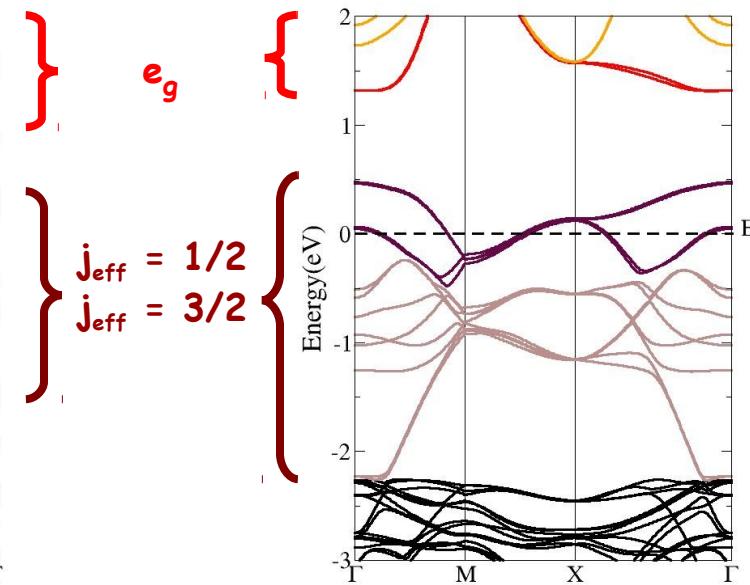


Baumberger et al.  
Phys Rev Lett 96, 246402 (2006)

- Spin-orbit coupling, electronic correlations and structural distortions are necessary to reproduce the Fermi surface within LDA+SO+U.

Haverkort et al, Phys Rev Lett 101, 026406 (2008)

Liu et al, Phys Rev Lett 101, 026408 (2008)

$\text{Sr}_2\text{RhO}_4$  (4d<sup>5</sup>) $\text{Sr}_2\text{IrO}_4$  (5d<sup>5</sup>)

- The Kohn-Sham band structure of  $\text{Sr}_2\text{RhO}_4$  and  $\text{Sr}_2\text{IrO}_4$  are qualitatively similar.  
But :
  - the bandwidths of  $\text{Sr}_2\text{RhO}_4$  are smaller than that of  $\text{Sr}_2\text{IrO}_4$ .
  - the spin-orbit splitting in  $\text{Sr}_2\text{RhO}_4$  is half of that of  $\text{Sr}_2\text{IrO}_4$ .

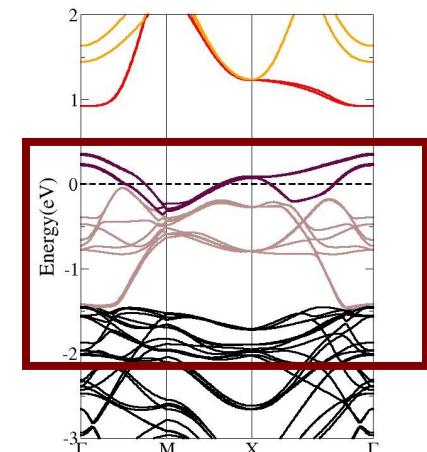
Rhodium (Rh)  
Iridium (Ir)

$\zeta_{SO} \sim 0.191$  eV  
 $\zeta_{SO} \sim 0.4$  eV

$\text{Sr}_2\text{RhO}_4$  has identical crystal structure as  $\text{Sr}_2\text{IrO}_4$

But smaller SO coupling 0.2

Charge repartition between the  $j_{\text{eff}}=1/2$  state  
and the two  $j_{\text{eff}}=3/2$  states are different.

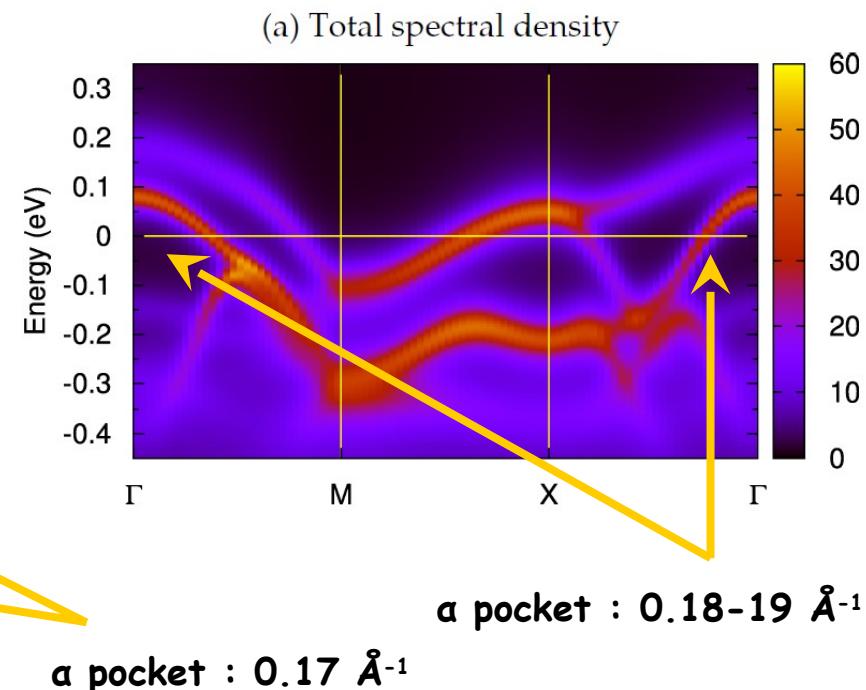
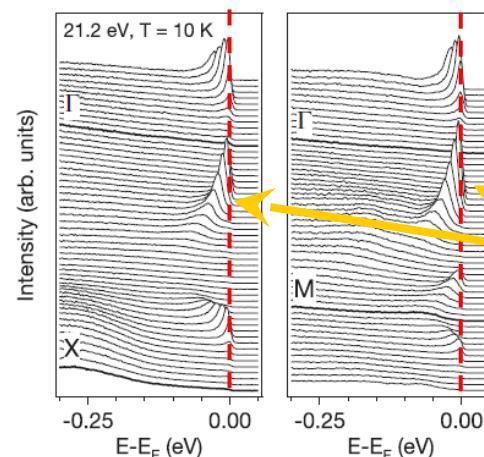
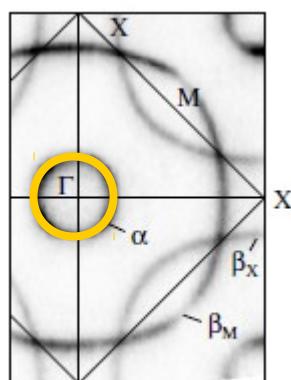


Charge	$\text{Sr}_2\text{IrO}_4$	$\text{Sr}_2\text{RhO}_4$
$j_{\text{eff}} = 1/2$	1.14	1.40
$j_{\text{eff}} = 3/2  m_j  = 1/2$	2.00	1.96
$j_{\text{eff}} = 3/2  m_j  = 3/2$	1.96	1.64

$\text{Sr}_2\text{RhO}_4$  is a “three-quarter-filled two-bands” system

**Sr<sub>2</sub>RhO<sub>4</sub> is a paramagnetic correlated metal.**  
(U = 1.6 eV and J = 0.3 eV)

Comparison with experimental spectral function obtained with ARPES (at 10K) :

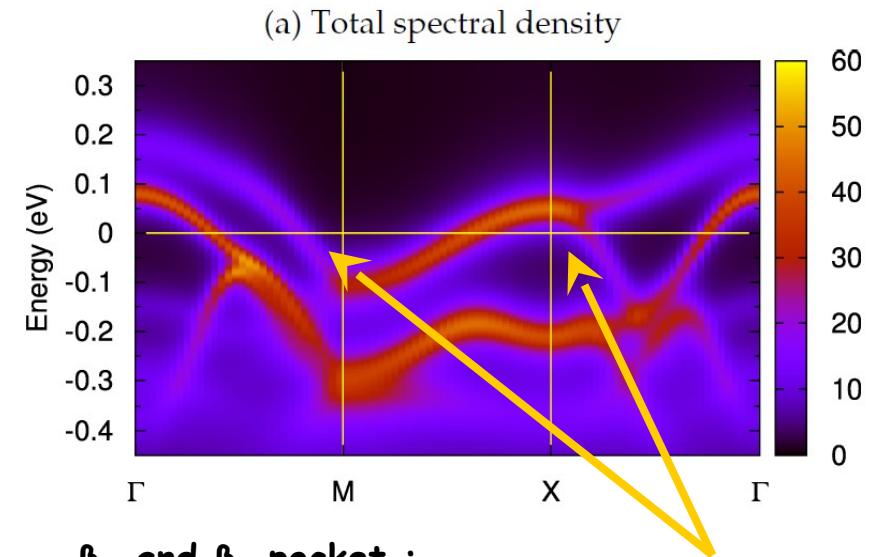
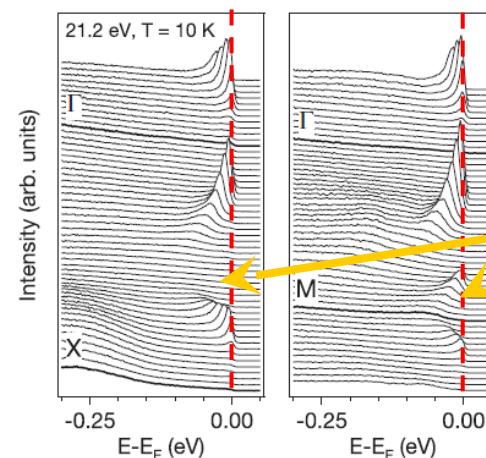
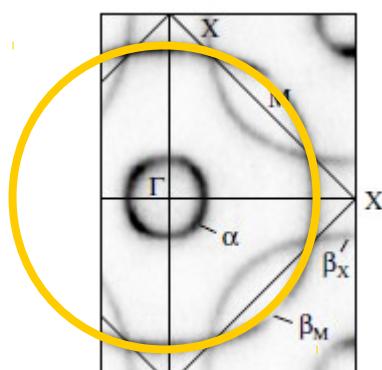


Baumberger et al., Phys Rev Lett 96, 246402 (2006)

Charge	LDA	LDA+DMFT
$j_{\text{eff}} = 1/2$	1.40	1.26
$j_{\text{eff}} = 3/2  m_j  = 1/2$	1.96	2.00
$j_{\text{eff}} = 3/2  m_j  = 3/2$	1.64	1.70

**Sr<sub>2</sub>RhO<sub>4</sub> is a paramagnetic correlated metal.**  
(U = 1.6 eV and J = 0.3 eV)

Comparison with experimental spectral function obtained with ARPES (at 10K) :

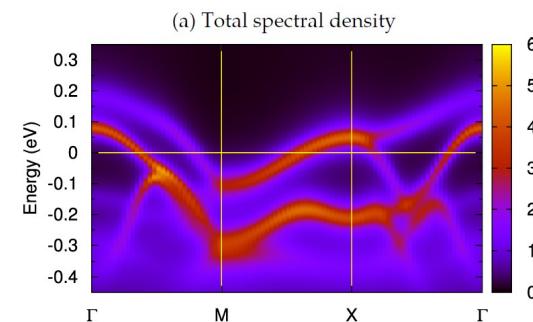
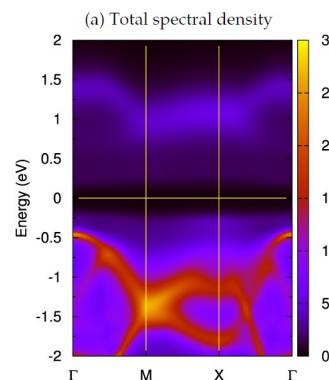


Baumberger et al., Phys Rev Lett 96, 246402 (2006)

Charge	LDA	LDA+DMFT
$j_{\text{eff}} = 1/2$	1.40	1.26
$j_{\text{eff}} = 3/2  m_j  = 1/2$	1.96	2.00
$j_{\text{eff}} = 3/2  m_j  = 3/2$	1.64	1.70

*Ab-initio* (LDA+SO+DMFT) calculations for  $\text{Sr}_2\text{IrO}_4$  and  $\text{Sr}_2\text{RhO}_4$  show that

- $\text{Sr}_2\text{IrO}_4$  is a  $j_{\text{eff}} = 1/2$  Mott insulator.
- $\text{Sr}_2\text{RhO}_4$  is a partially spin-orbital polarized metal.



Difference due to different strength of Spin-Orbit coupling!



Cyril Martins



Loig Vaugier



Silke Biermann